



Repairing Entities using Star Constraints in Multi-relational Graphs

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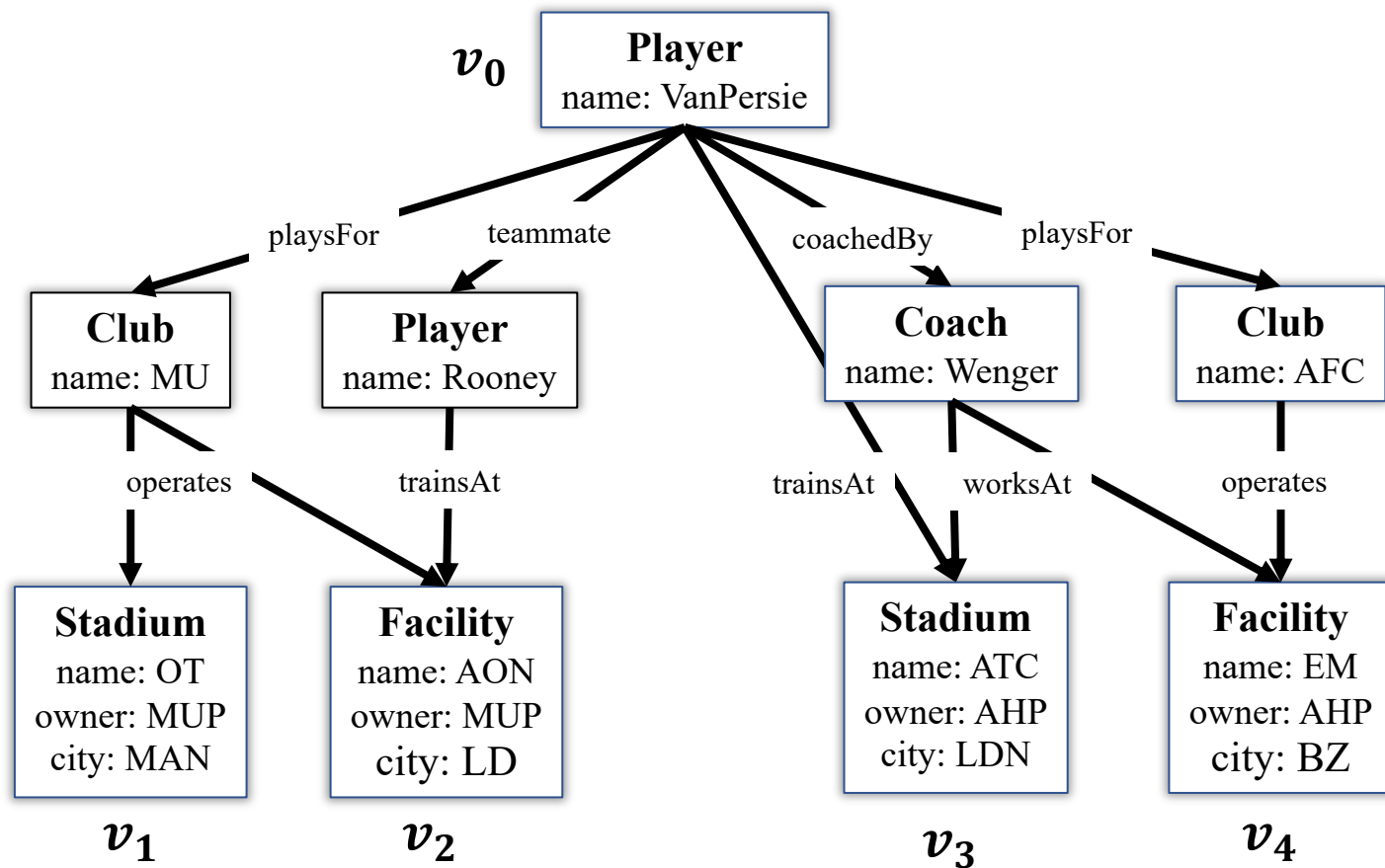
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NATIONAL LABORATORY

Erroneous entities: how to capture?

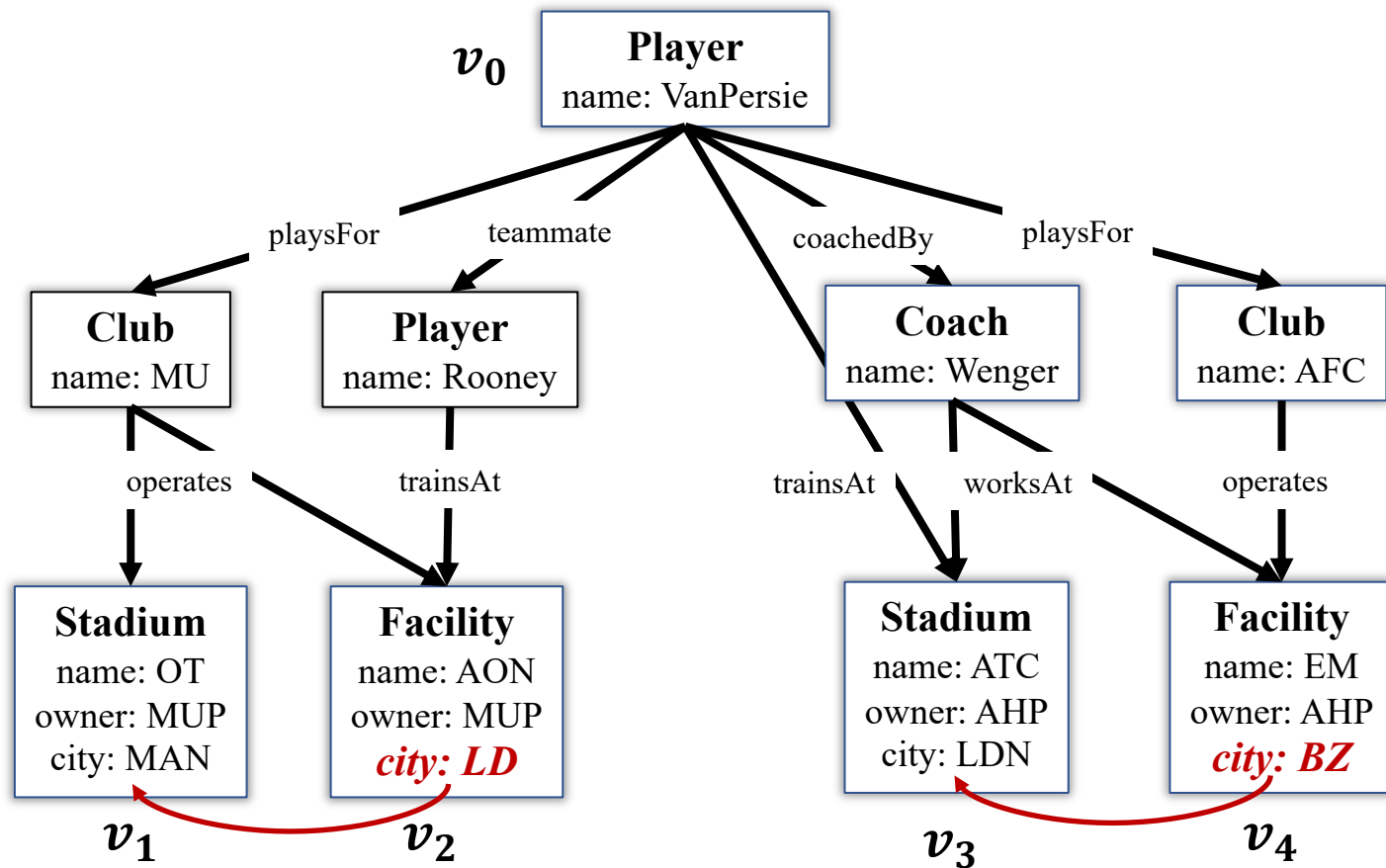
- Multi-relational graphs: a labeled graph with attributes on nodes



Graph G: a football database

Erroneous entities: how to capture?

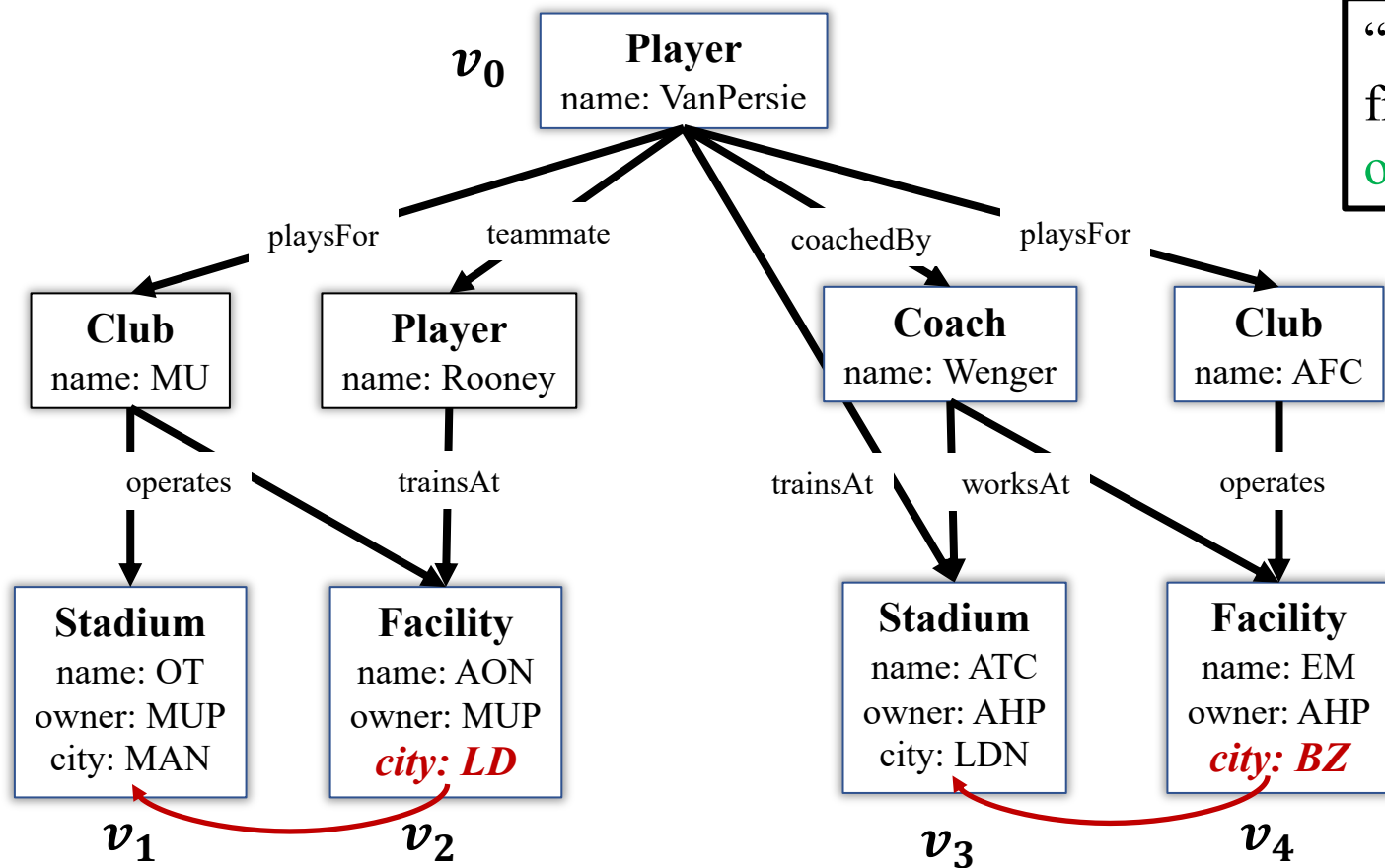
- Multi-relational graphs: a labeled graph with attributes on nodes
- Entity errors: incorrect node attributes



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Erroneous entities: how to capture?

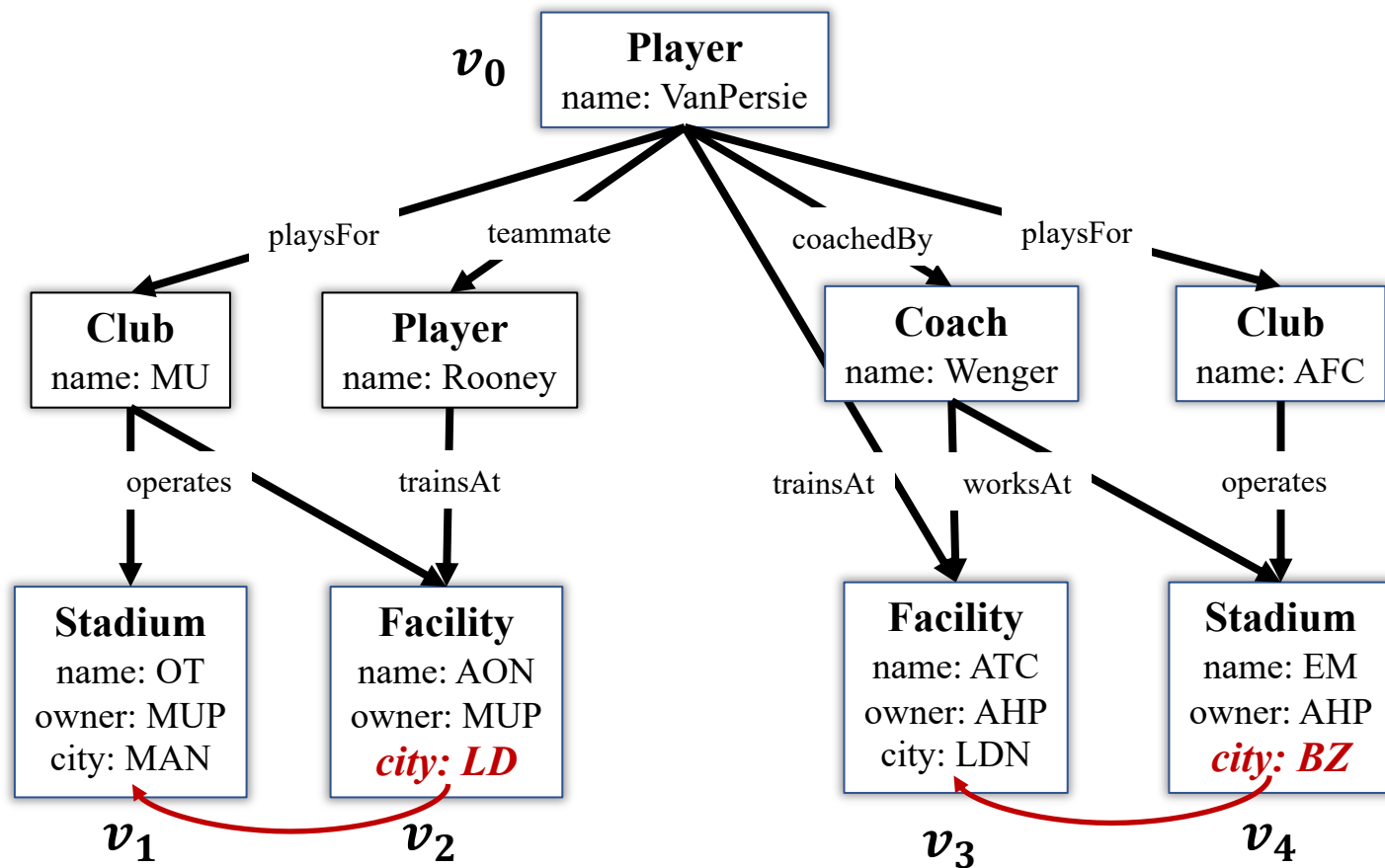
- Multi-relational graphs: a labeled graph with attributes on nodes
- Entity errors: incorrect node attributes
- Semantics: *relevant paths from a center node*



“For **stadium** and **facility** *relevant* to **player** (v_0) from **Premier League**, if they have the same **owner**, then they should locate at the same **city**.”

Regular path queries

- Regular expressions: $R = l \mid l^{\leq k} \mid R \cdot R \mid R \cup R$

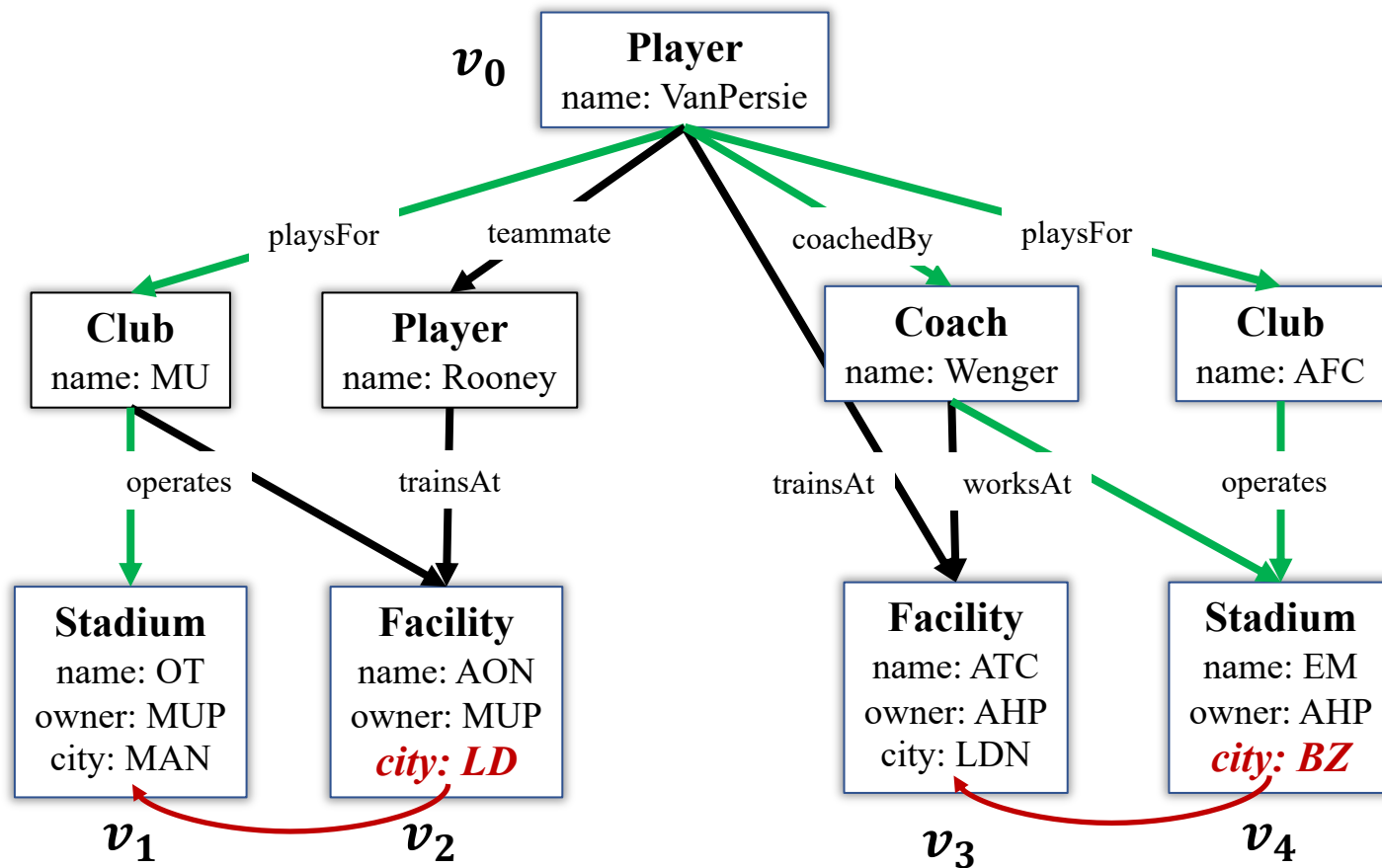


Graph G: a football database

Regular path queries

- Regular expressions: $R = l \mid l^{\leq k} \mid R \cdot R \mid R \cup R$

- Paths from **Player** to **Stadium**
- $R_1 = (\text{playsFor} \cdot \text{operates}) \cup (\text{coachedBy} \cdot \text{worksAt})$



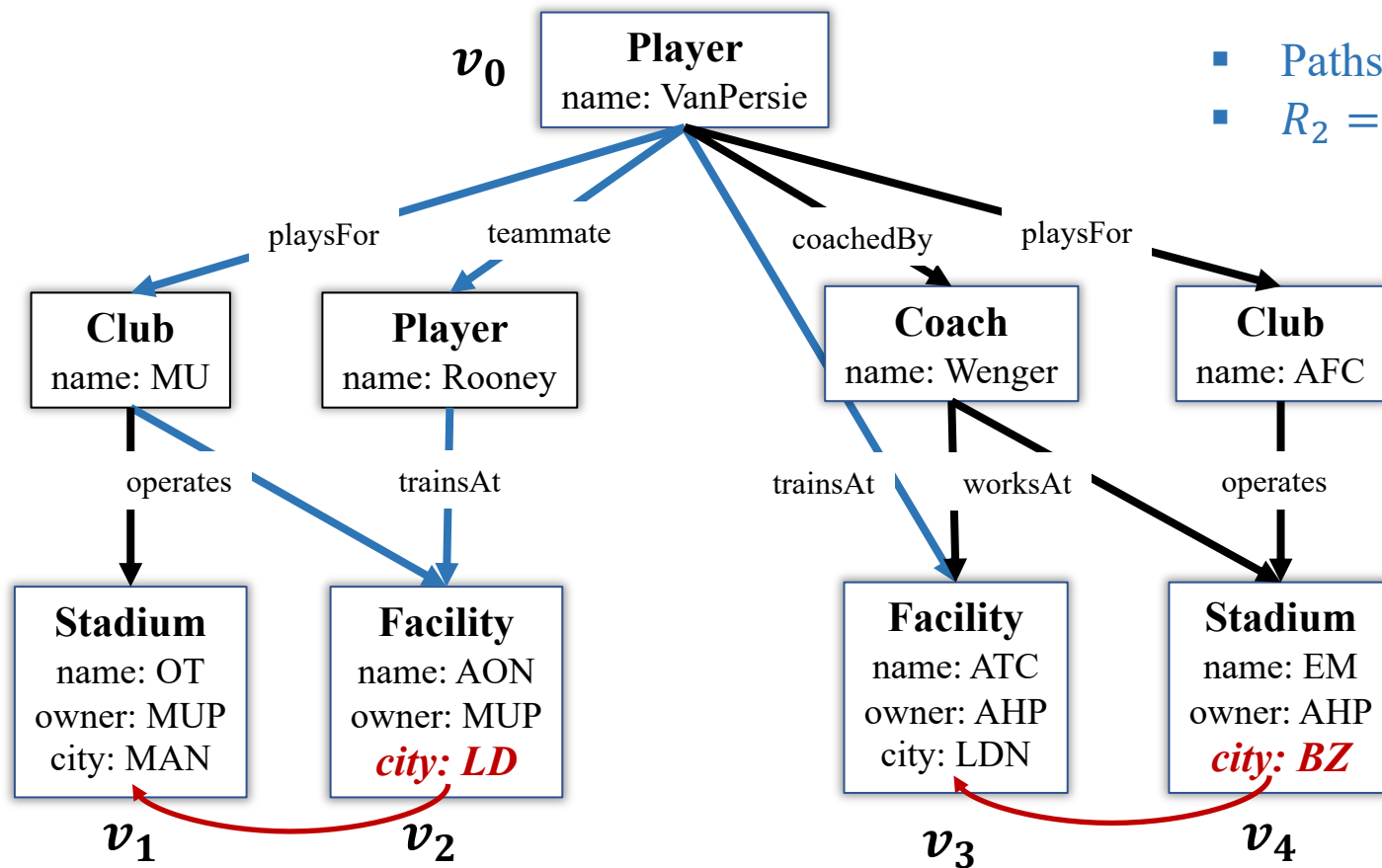
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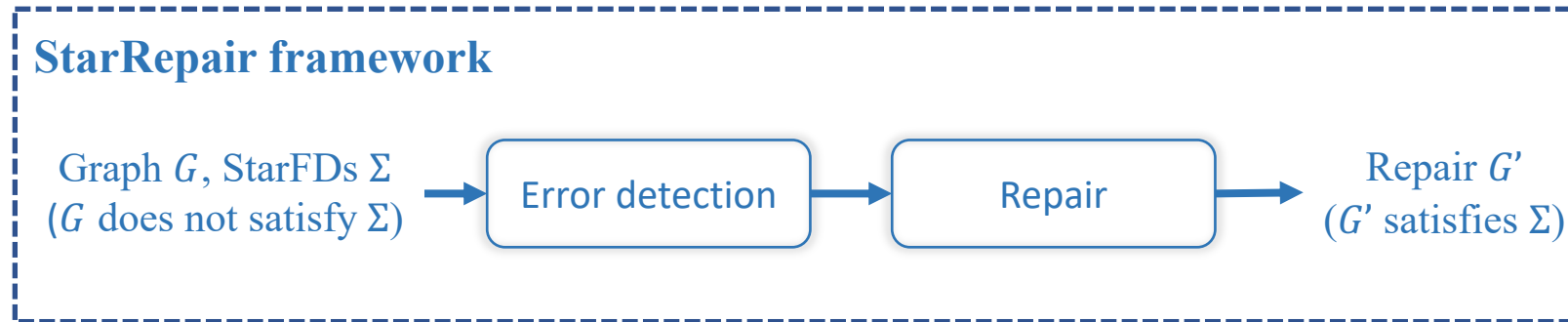
- Paths from **Player** to **Stadium**
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- Paths from **Player** to **Facility**
- $R_2 = (\text{playsFor} \cdot \text{operates}) \cup (\text{teammate}^{\leq 1} \cdot \text{trainsAt})$



Graph G: a football database

Contributions



Contributions

StarFDs: star functional dependencies
new constraints for graphs

Entity repair problem: minimum
editing cost, NP-hard and APX-hard

StarRepair framework



Feasible framework with provable
guarantees whenever possible

Contributions

StarFDs: star functional dependencies
new constraints for graphs

Entity repair problem: minimum
editing cost, NP-hard and APX-hard

StarRepair framework

Graph G , StarFDs Σ
(G does not satisfy Σ)

Error detection

Repair

Repair G'
(G' satisfies Σ)

Feasible framework with provable
guarantees whenever possible

Repair workflow

Is approximable?

Yes

No

Is optimal repairable?

Heuristic solution

Yes

No

Optimal solution

Approximation solution

Star constraints

- **StarFDs:** $\varphi = (P(u_o), X \rightarrow Y)$

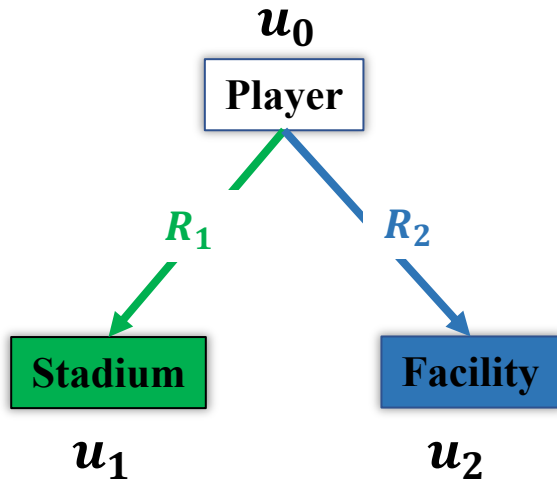
- Star pattern $P(u_o)$:

- Value constraints: $X \rightarrow Y$

Star constraints

- StarFDs: $\varphi = (P(u_o), X \rightarrow Y)$

- Star pattern $P(u_o)$:
 - A two-level tree with center node u_o
 - Each branch is a regular expression



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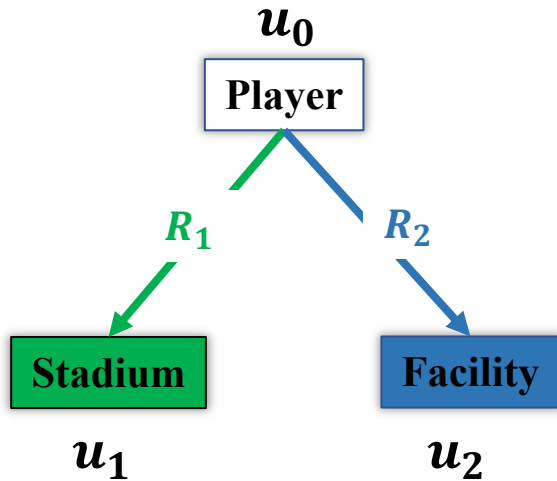
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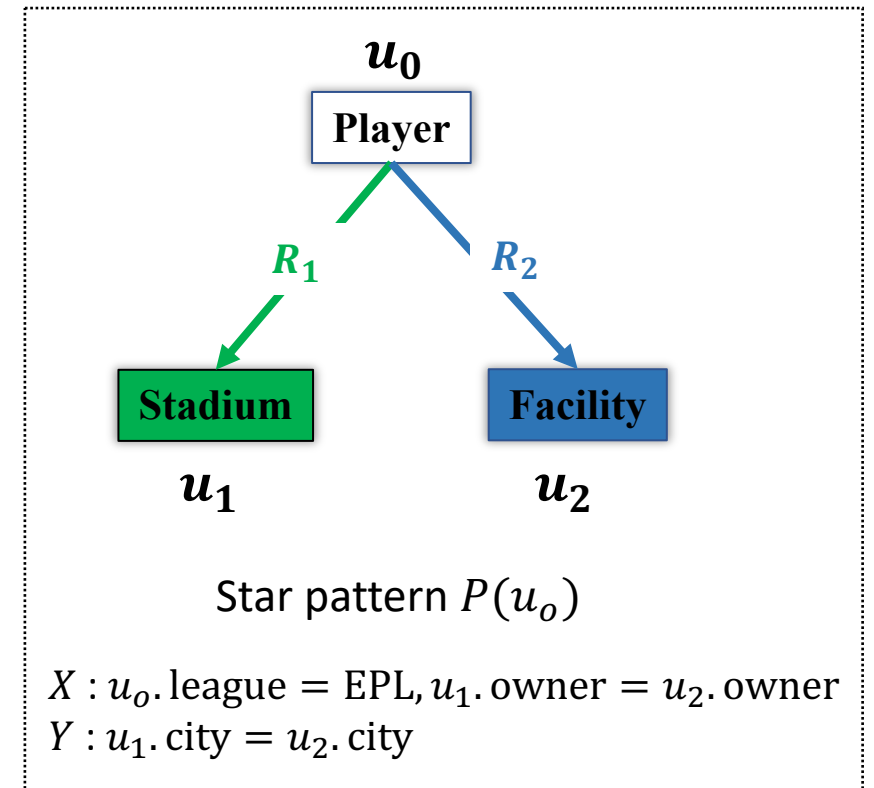
- X and Y are two sets of literals
- Literals: $u.A = c$, or $u.A = u'.A'$

$X : u_o.\text{league} = \text{EPL}, u_1.\text{owner} = u_2.\text{owner}$

$Y : u_1.\text{city} = u_2.\text{city}$

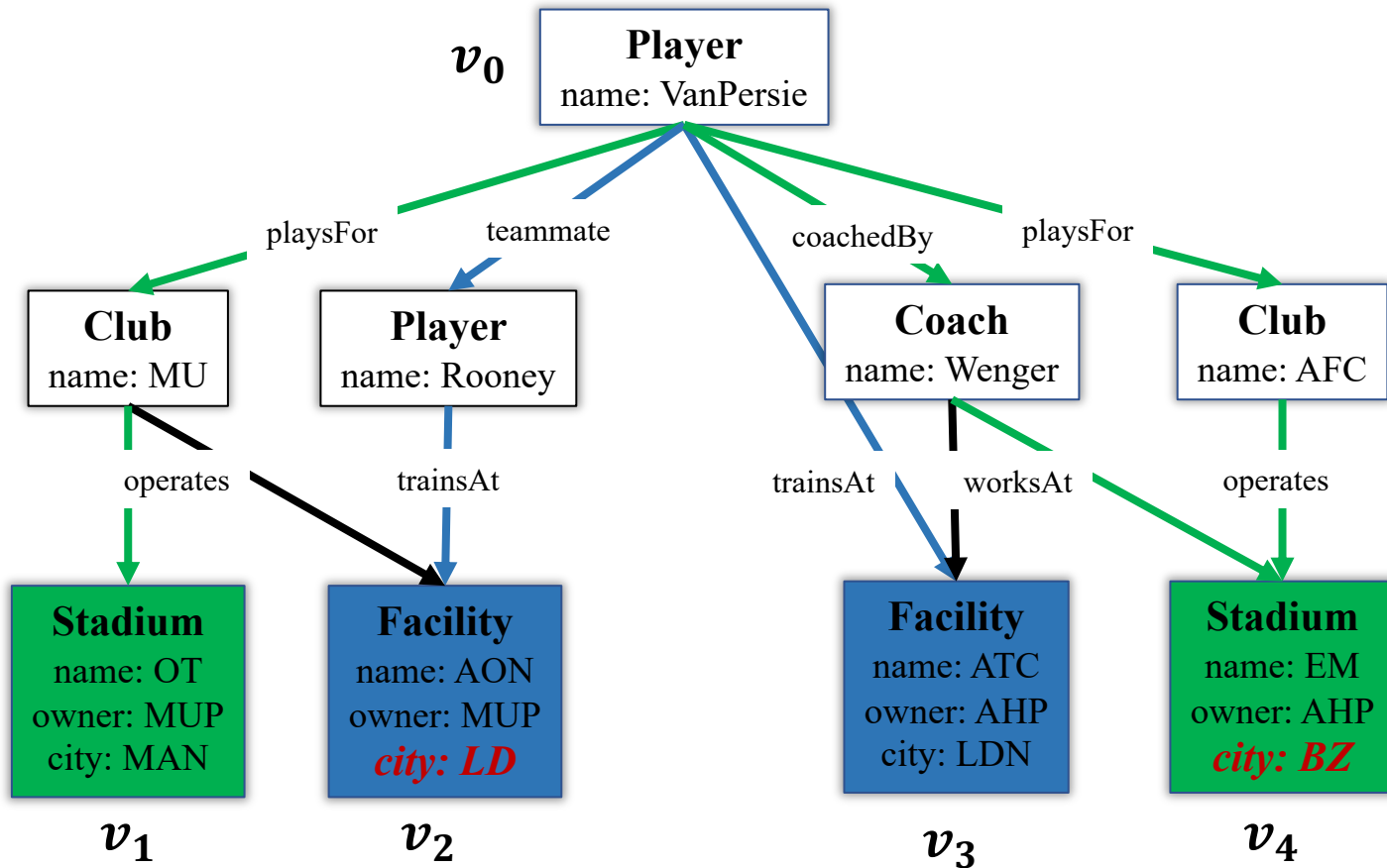
Star constraints

- Matching semantics: maximum set matched by star pattern

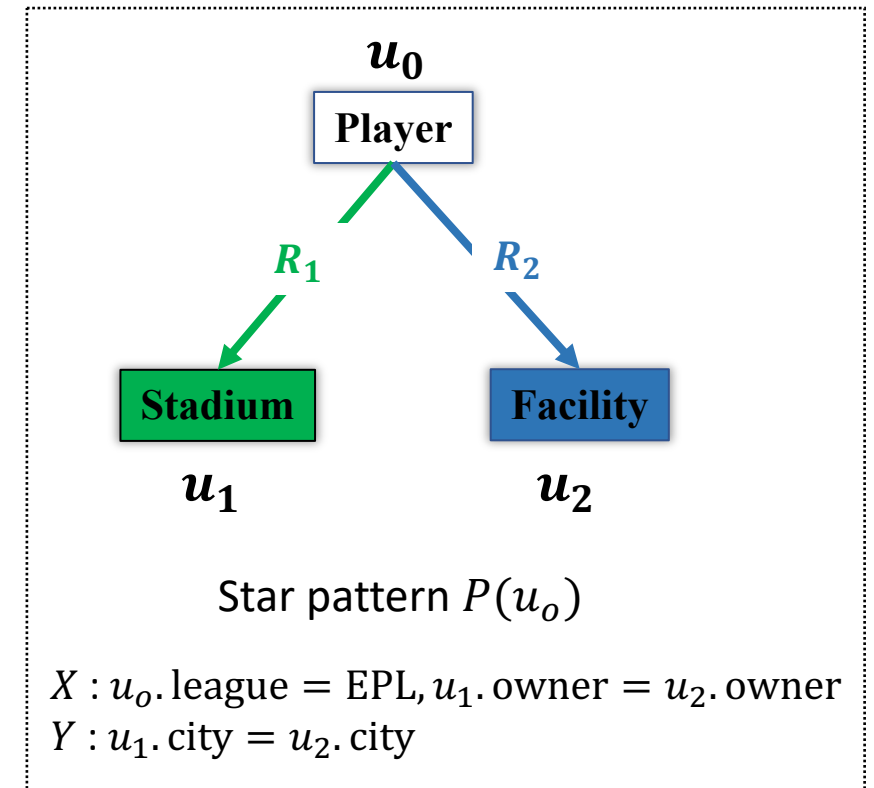


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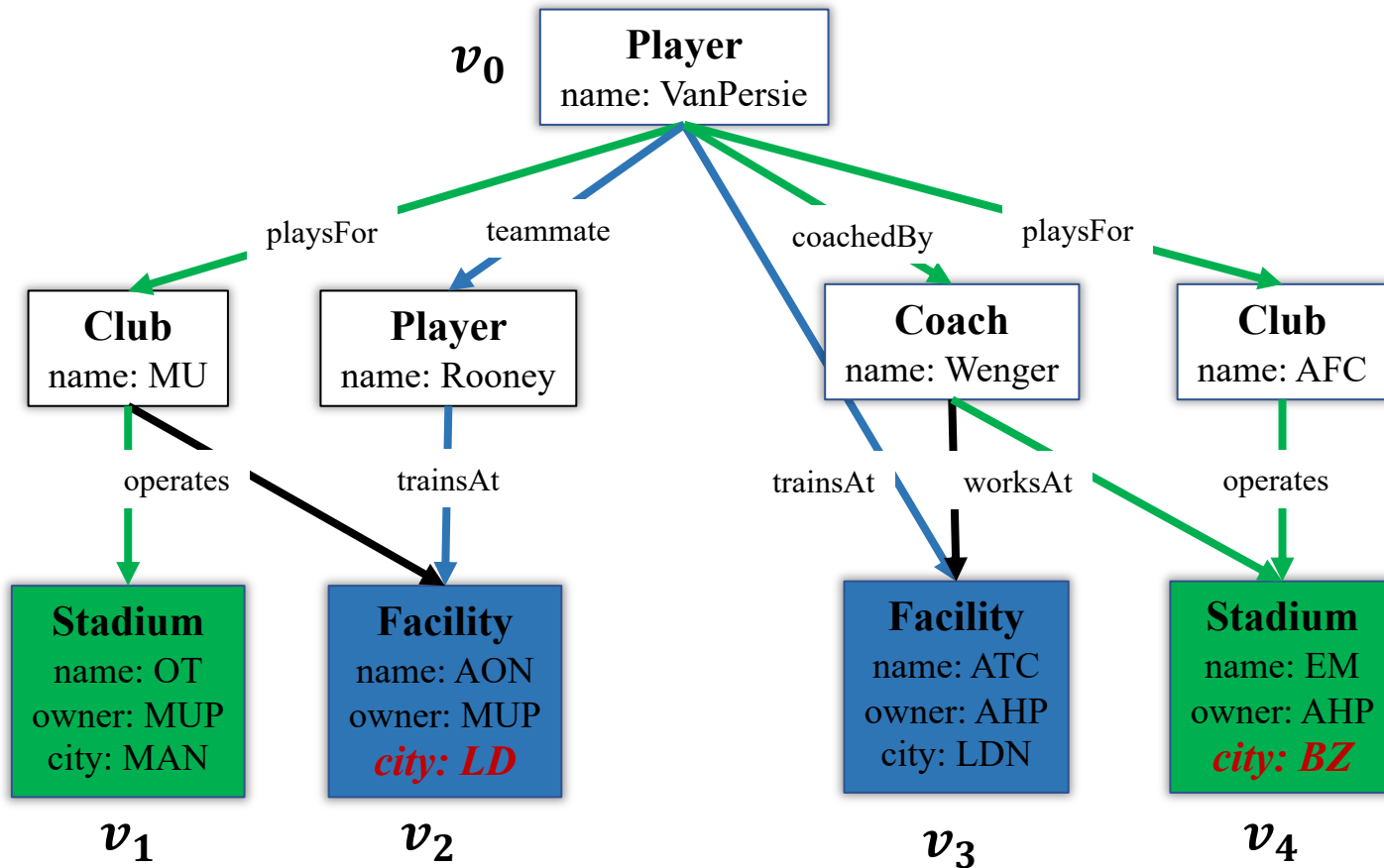


u_0 matches v_0
 u_1 matches v_1 and v_4
 u_2 matches v_2 and v_3

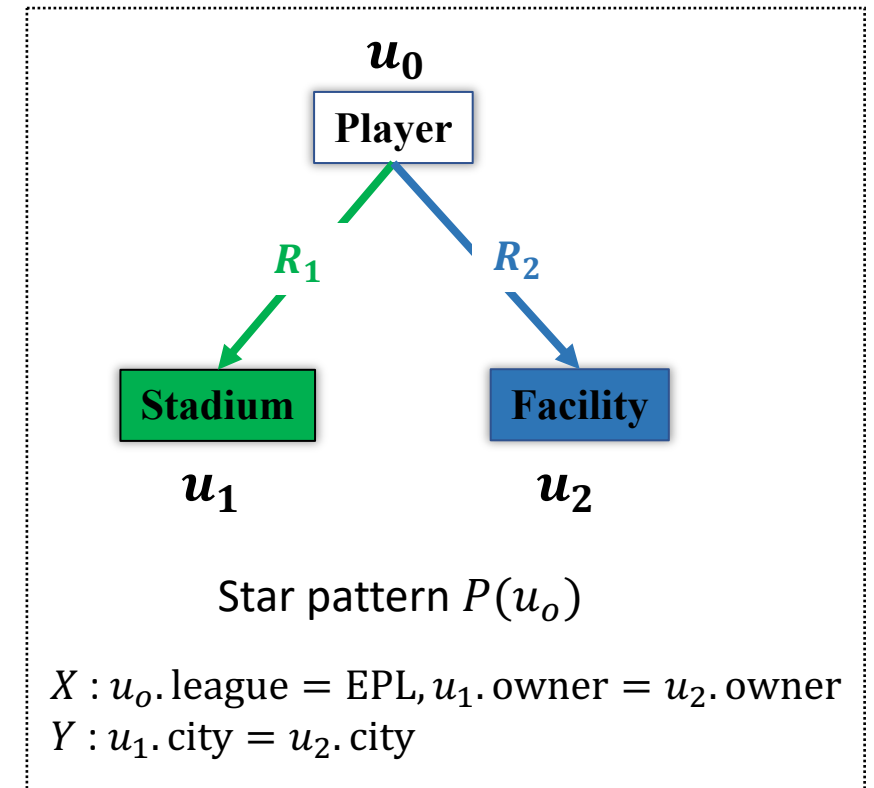


Star constraints

- Matching semantics: maximum set matched by star pattern
- Inconsistencies I : matches that X holds but Y does not hold



u_0 matches v_0
 u_1 matches v_1 and v_4
 u_2 matches v_2 and v_3



Summary of results

Problem	Description	Hardness	Solution
Satisfiability	Input: Σ decide whether there exists G that satisfies Σ	NP-complete	
Implication	Input: Σ and φ decide whether for all G satisfy Σ , they satisfy φ	coNP-hard	
Error detection (validation)	Input: G and Σ Output: all inconsistencies I	PTIME	Evaluate regular path queries and validate values - time complexity: $O(\Sigma V + V (V + E))$
Repair	Input: Σ and G that does not satisfy Σ Output: G' that satisfies Σ with least repair cost	NP-hard APX-hard	Approximable cases (PTIME checkable) - time complexity $O(I \Sigma ^2 + I (I \Sigma ^2 + I \Sigma))$ - approximation ratio: $ I \Sigma ^2$
			Optimal cases - time complexity $O(I \Sigma)$
			Heuristic cases - time complexity $O(I \Sigma ^2 + I (I \Sigma ^2 + I \Sigma))$ - bounded repairable: cost $\leq I $

- Notations
 - G : graph
 - Σ : a set of StarFDs
 - V : nodes
 - φ : a single StarFD
 - E : edges
 - I : all inconsistencies.

Updates and repairs

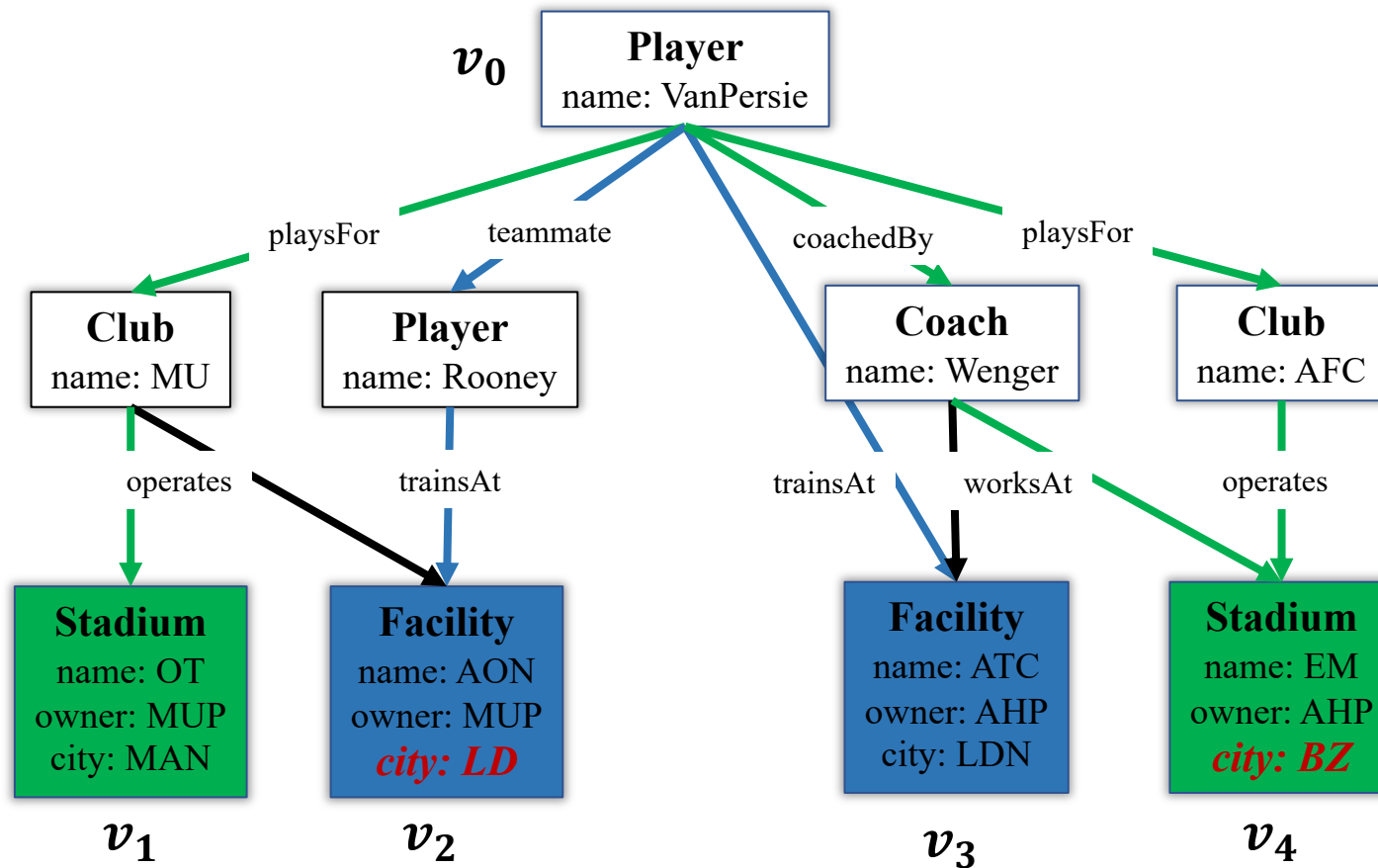
- Updates O : operators $o = (v.A, a, c)$ with editing cost
- Repair O : applying O to G , such that obtain G' that satisfies Σ

$$\text{cost}(O) = \sum_{o \in O} \text{cost}(o)$$

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Two repairs:

$O_1 = \{(v_2.\text{city}, \text{LD}, \text{MAN}), (v_4.\text{city}, \text{BZ}, \text{LDN})\}$

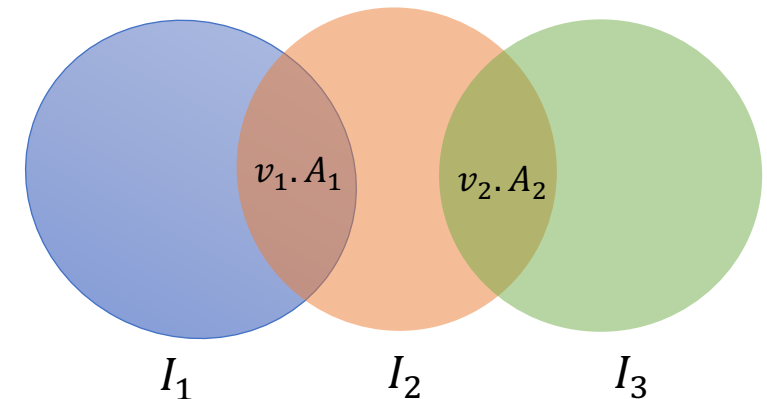
$O_2 = \{(v_2.\text{owner}, \text{MUP}, \text{CFG}), (v_4.\text{owner}, \text{EM}, \text{ENIC})\}$

Entity repair problem

- **Input:** StarFDs Σ , and graph G does not satisfy Σ
- **Output:** a repair O , such that
 - obtain G' that satisfies Σ
 - $\text{cost}(O) \leq \text{cost}(O')$ for any O'

Entity repair problem

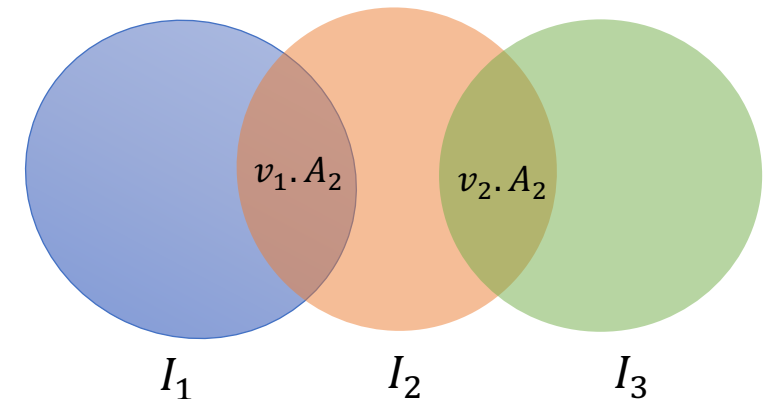
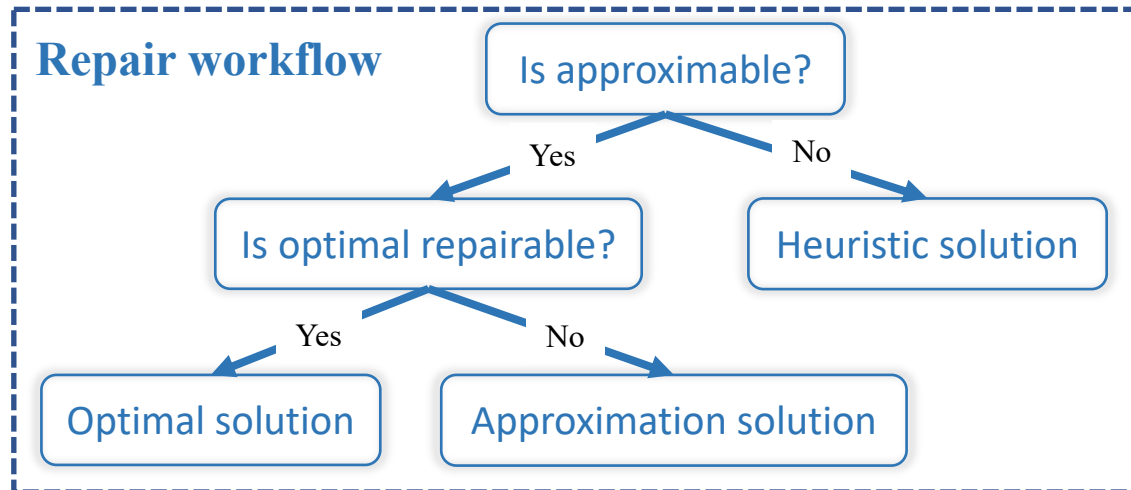
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- Solution overview
 - Connected components (CCs): inconsistencies connected at shared node attributes
 - Isolated CCs: no new inconsistency is introduced when a CC is repaired



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Isolated CCs have approximate solutions

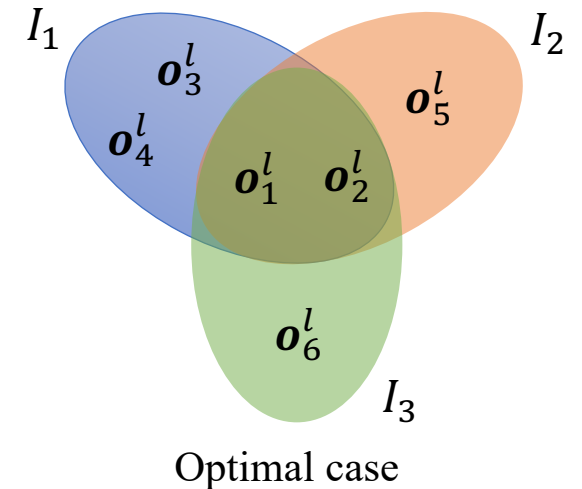
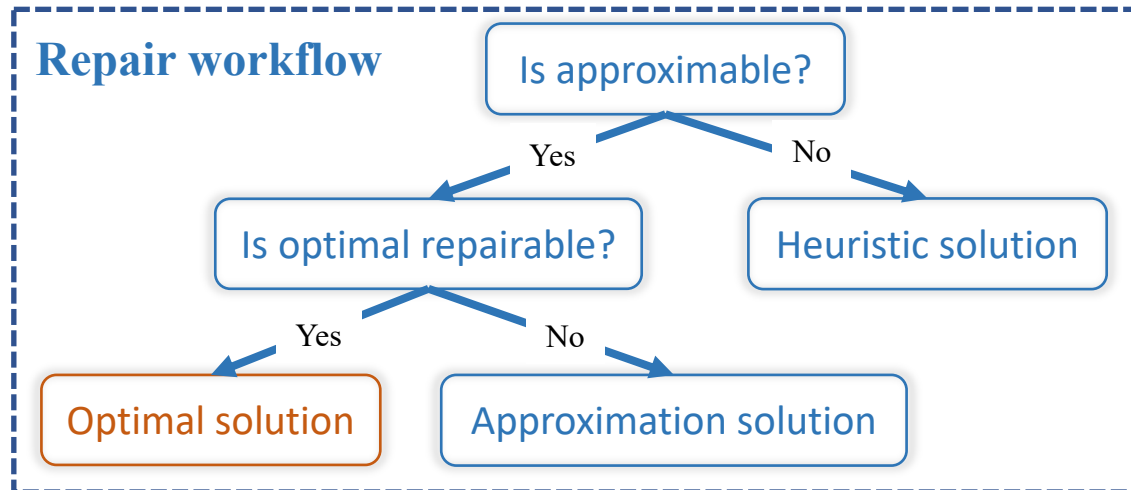


Optimal case

- Updates \mathbf{o}^l : flip the condition of a literal l in $X \cup Y$
- Optimal solution: hyper star structure
 - Select the \mathbf{o}^* with least cost in center
 - Select one \mathbf{o} with least cost in each petal, and induce \mathbf{O}
 - If $\text{cost}(\mathbf{o}^*) \leq \text{cost}(\mathbf{O})$, return \mathbf{o}^* ; otherwise, return \mathbf{O}

Example:

- $\mathbf{o}^* = \mathbf{o}_1^l$
- $\mathbf{O} = \mathbf{o}_3^l \cup \mathbf{o}_5^l \cup \mathbf{o}_6^l$
- Return \mathbf{o}^* that has less cost

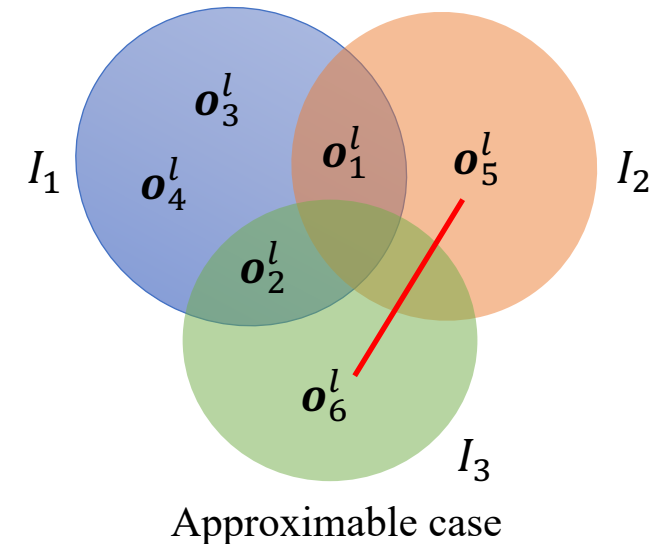
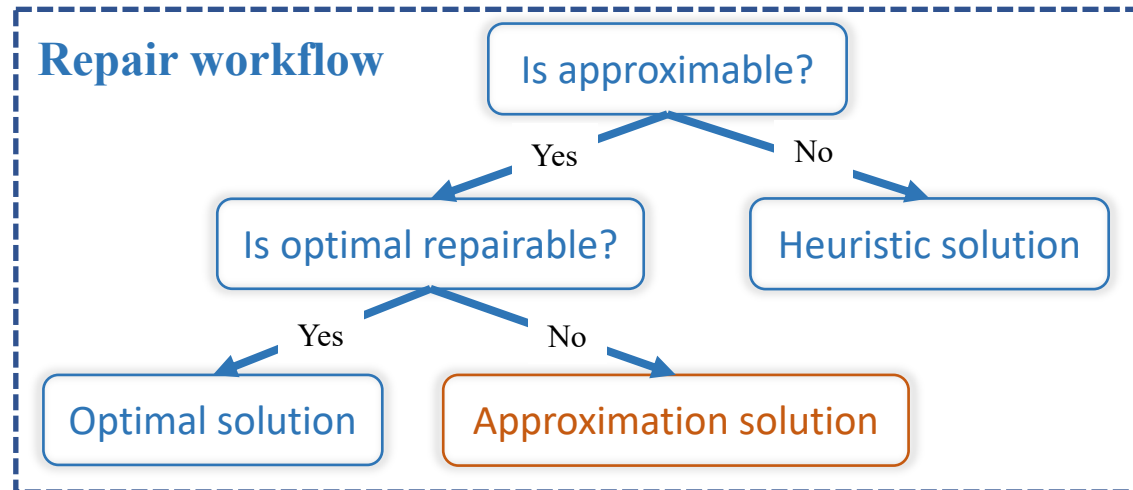


Approximable case

- Updates \mathbf{o}^l : flip the condition of a literal l in $X \cup Y$
- Approximation solution:
 - Hypergraph vertex cover without forbidden pairs
 - Forbidden pairs
 - $\mathbf{o}_5^l = \{(v_2.\text{owner}, \text{MUP}, \text{CFG}), (v_4.\text{owner}, \text{EM}, \text{ENIC})\}$
 - $\mathbf{o}_6^l = \{(v_2.\text{owner}, \text{MUP}, \text{FSG}), (v_4.\text{owner}, \text{EM}, \text{ENIC})\}$

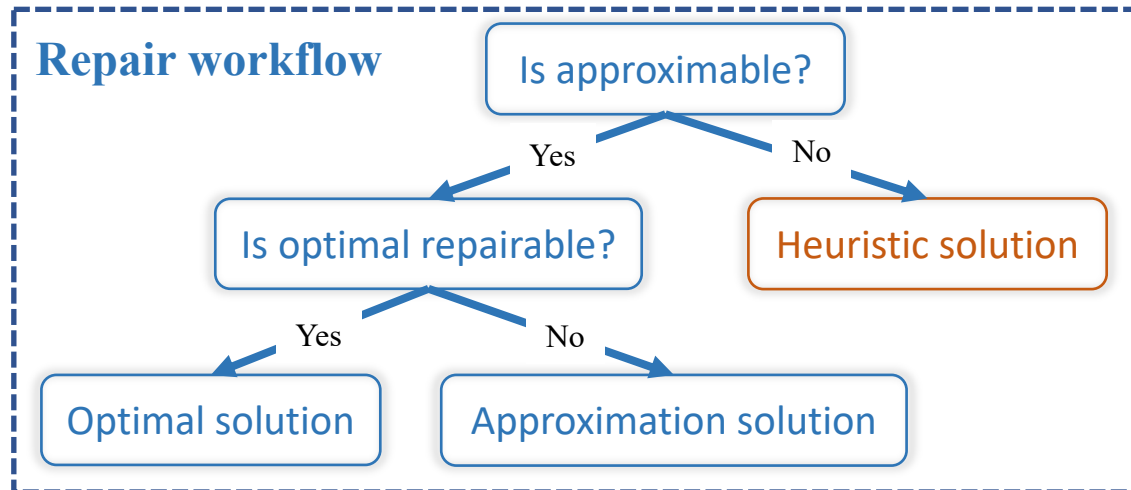
Example:

- Return $\mathbf{O} = \mathbf{o}_2^l \cup \mathbf{o}_5^l$
- \mathbf{o}_6^l is pruned

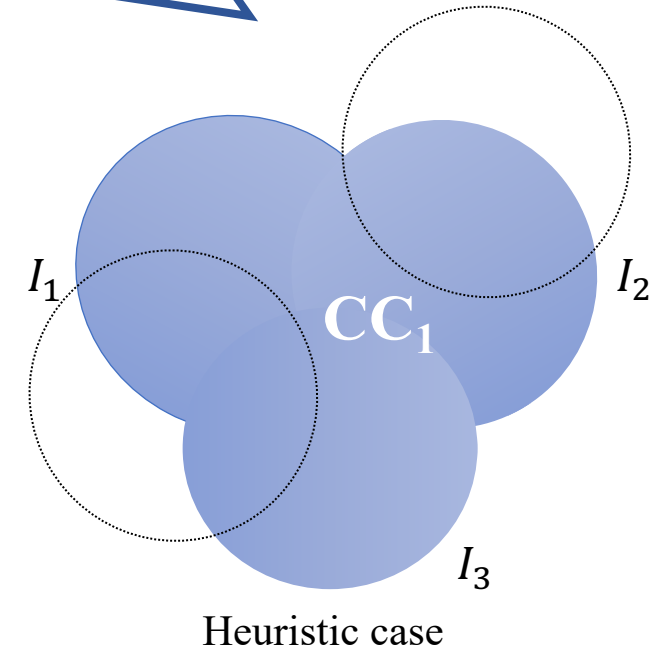


Heuristic case

- Updates \mathbf{o}^l : flip the condition of a literal l in $X \cup Y$
- Heuristic solution (for *non-isolated* CC):
 - Select CC introducing fewest inconsistencies
 - Invoke approximation/optimal solution
 - Re-detect inconsistencies
 - Repeat until incur a cost bound

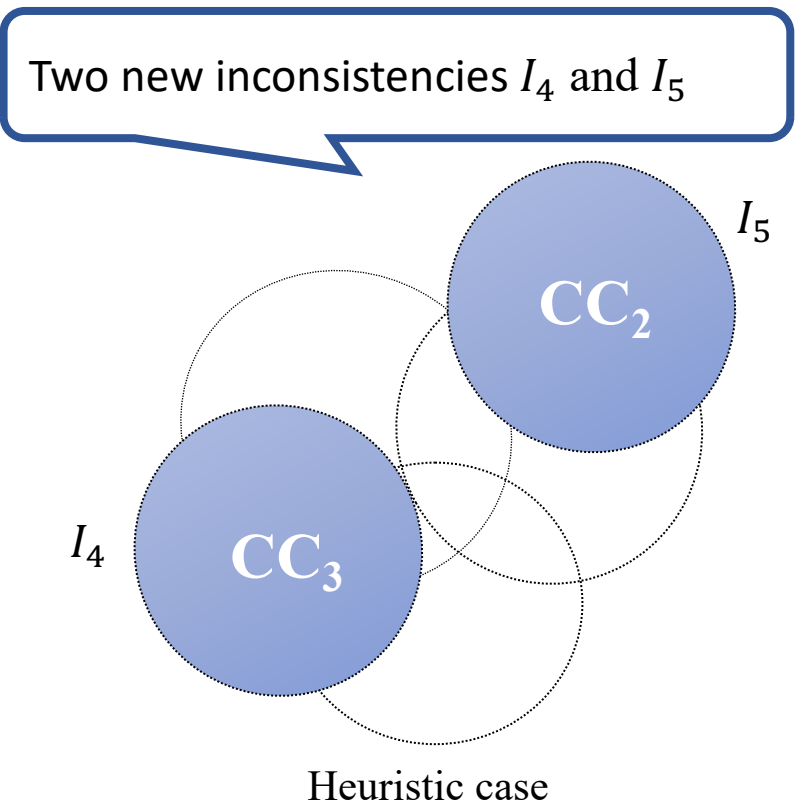
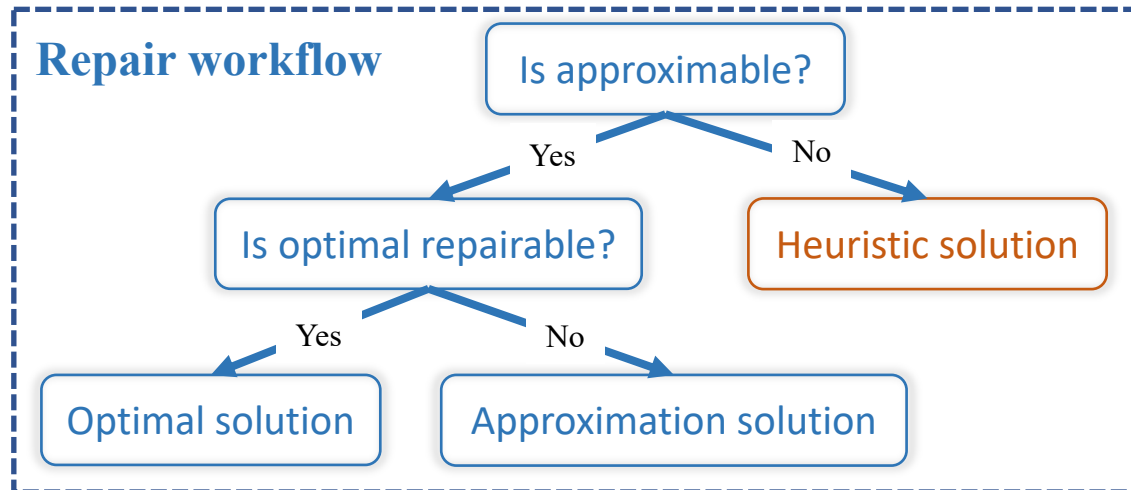


Repair CC_1 consisting of I_1 , I_2 , and I_3



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Experiment settings

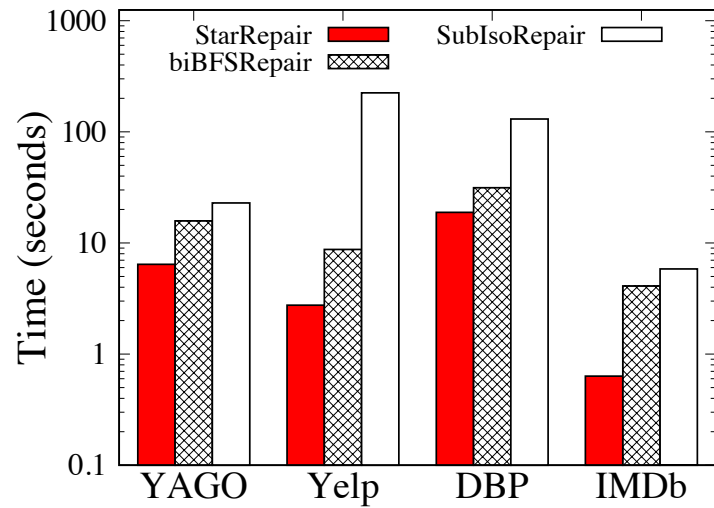
- Datasets

Data	Description	# of nodes	# of edges	avg. # of attributes per node
Yago	Knowledge graph	2.1M	4.0M	3
DBPedia	Knowledge graph	2.2M	7.4M	4
Yelp	Business reviews	1.5M	1.6M	5
IMDb	Movie network	5.9M	3.2M	3

- Error generation: adopt silver standard and an error generation benchmark (Arocena et al. 2015)
- StarFD generation: discovered from silver standard (first star patterns and then value constraints)
- Algorithms:
 - **StarRepair:** use bidirectional search for regular path queries with incremental error detection
 - **biBFSRepair:** use bidirectional search *without incremental error detection*
 - **SubIsoRepair:** *use subgraph isomorphism* as matching semantics with incremental error detection

Experiment results

- StarFD repairs: efficiency and effectiveness

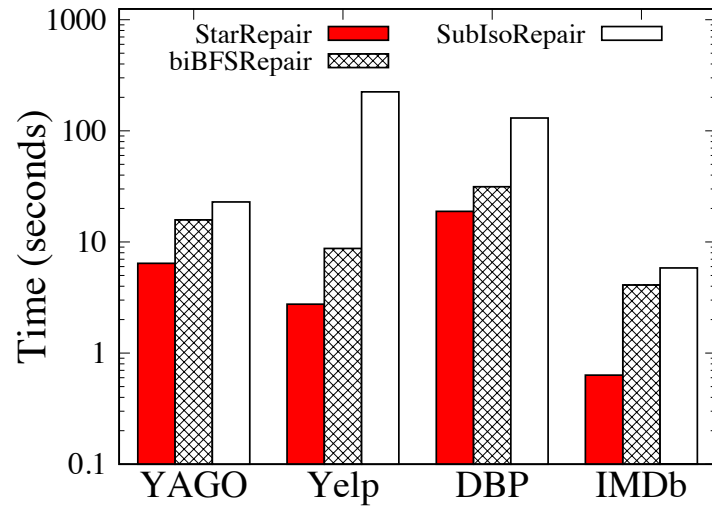


StarRepair outperforms biBFSRepair and SubIsoRepair by 3.4 and 7.1 times respectively

- Case study

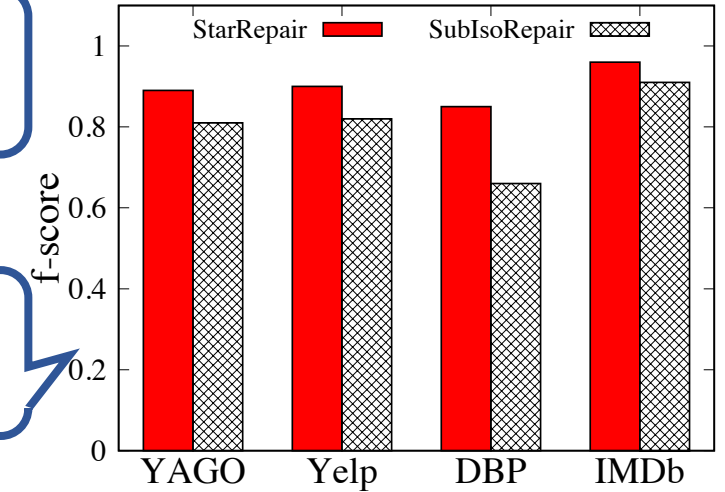
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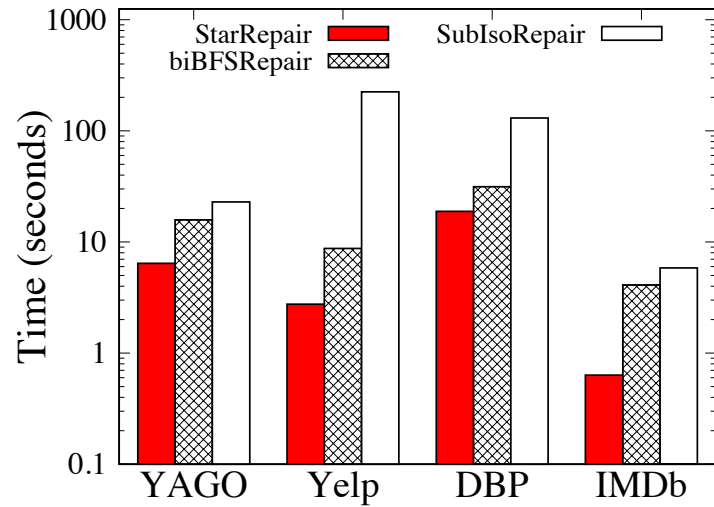
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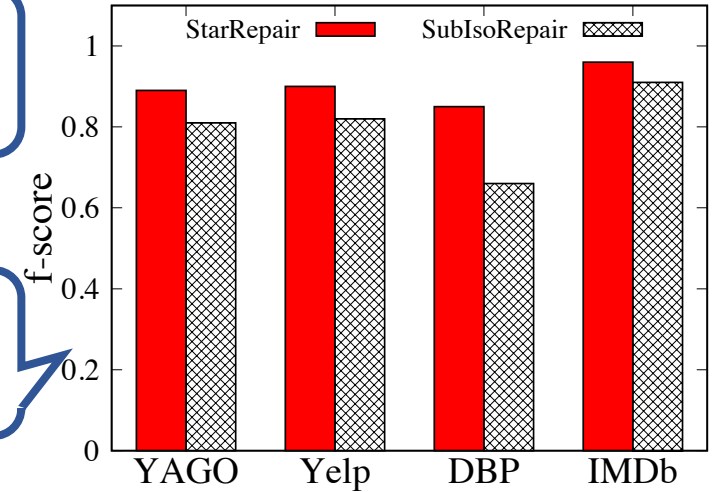
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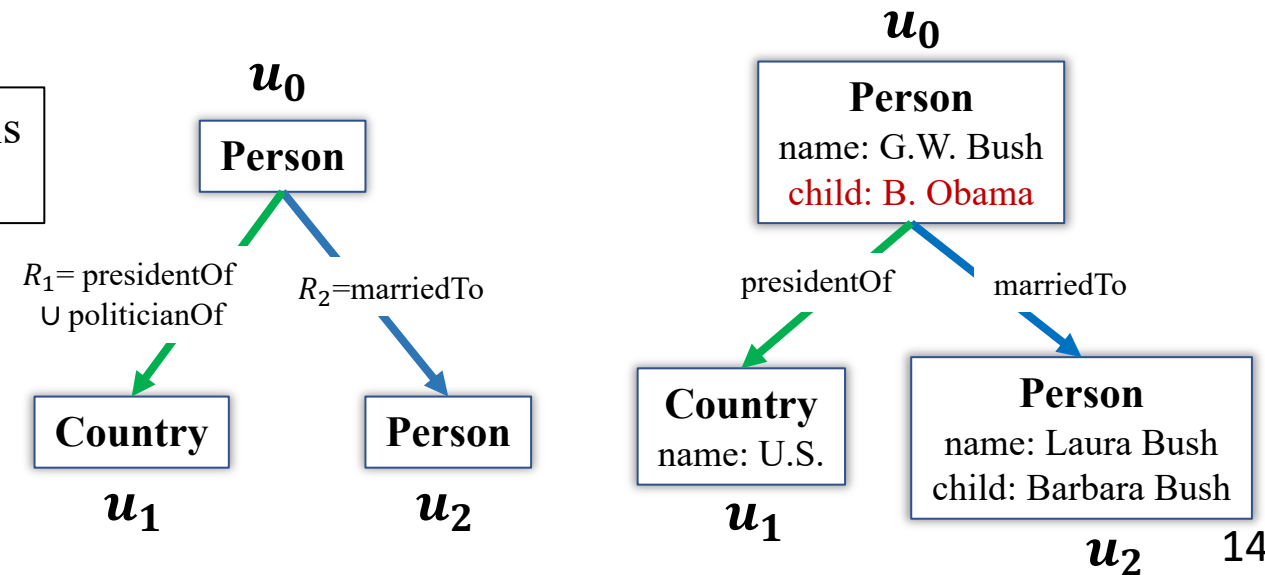
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Case study

StarFD: If a person u_0 is a politician or president of U.S., and is married to another person u_1 , then u_1 's child is u_0 's child.

We found more than 100 such errors in Yago.



Compare with GFDs (Fan et al. 2016)

- StarFDs: star functional dependencies
 - Definition: $\varphi = (P(u_o), X \rightarrow Y)$
- GFDs: graph functional dependencies
 - Definition: $\varphi = (P, X \rightarrow Y)$

Problem	StarFDs	GFDs
Semantic	star patterns with regex queries	subgraph isomorphism
Satisfiability	NP-complete	coNP-complete
Implication	coNP-hard	NP-complete
Error detection (validation)	PTIME	coNP-complete

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Kronos: Lightweight Knowledge-based Event Analysis in Cyber-Physical Data Streams
To appear in Demo Session